

$$n_1, n_2 \geq 10$$

① Mann Whitney U test:

$$U_1 = n_1 n_2 + \frac{n_1(n_1+1)}{2} - R_1$$

$$U_2 = n_1 n_2 + \frac{n_2(n_2+1)}{2} - R_2$$

$$Z = \frac{U - n_1 n_2 / 2}{\sqrt{n_1 n_2 (n_1 + n_2 + 1) / 12}}$$

Large samples use  $Z = \frac{U - \mu_U}{\sigma_U}$   
 $n_1, n_2 \geq 10$

$$U = \text{Min}(U_1, U_2)$$

$n_1, n_2$  = Size of samples

$R_1, R_2$  = Rank Sums.

① From the following table use mann whitney U test to determine whether there is a difference in the course of the 2 groups. Use 0.05 LOS (large).

Grp A	Grp B
7	8
11	9
9	13
4	14
8	11
6	10
12	12
11	14
9	13
10	9
11	10
	8

Sol:  $H_0$  - There is no diff b/w 2 grps  
 $H_1$  - There is diff b/w 2 grps

GA	GB	GA Arrange small-big	GB Arrange small-big	Ranks	Common Ranks
		4	-	1	1
		6	-	2	2
		7	-	3	3
		8	8, 8	4, 5, 6	$\frac{4+5+6}{3} = 5$
		9, 9	9, 9	7, 8, 9, 10	$\frac{7+8+9+10}{4} = 8.5$
		10	10, 10	11, 12, 13	12
		11, 11, 11	11	14, 15, 16, 17	15.5
		12	12	18, 19	18.5
		-	13, 13	20, 21	20.5
		-	14, 14	22, 23	22.5
RANKS		$n_1 = 11$	$n_2 = 12$		

Grp (A)  
Common  
Rank x Digits

Grp (B)  
Common  
Rank x Digit

$$\begin{aligned}
 1 \times 1 &= 1 \\
 2 \times 1 &= 2 \\
 3 \times 1 &= 3 \\
 5 \times 1 &= 5 \\
 8.5 \times 2 &= 17 \\
 12 \times 1 &= 12 \\
 15.5 \times 3 &= 46.5 \\
 18.5 \times 1 &= 18.5 \\
 &=
 \end{aligned}$$

$$\begin{aligned}
 &- \\
 &- \\
 &- \\
 5 \times 2 &= 10 \\
 8.5 \times 2 &= 17 \\
 12 \times 2 &= 24 \\
 15.5 \times 1 &= 15.5 \\
 18.5 \times 1 &= 18.5 \\
 20.5 \times 2 &= 41 \\
 22.5 \times 2 &= 45
 \end{aligned}$$

$$R_1 = 105$$

$$R_2 = 171$$

$$\begin{aligned}
 U_1 &= n_1 n_2 + \frac{n_1(n_1+1)}{2} - R_1 \\
 &= 11 \times 12 + \frac{11(11+1)}{2} - 105 \\
 &= 93
 \end{aligned}$$

$$\begin{aligned}
 U_2 &= n_1 n_2 + \frac{n_2(n_2+1)}{2} - R_2 \\
 &= 11 \times 12 + \frac{12(12+1)}{2} - 171 \\
 &= 39
 \end{aligned}$$

$$\begin{aligned}
 U &= \min(U_1, U_2) \\
 &= \min(93, 39)
 \end{aligned}$$

$$U = \underline{\underline{39}}$$

$$\begin{aligned}
 Z_{cal} &= \frac{U - n_1 n_2 / 2}{\sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{12}}} \\
 &= \frac{39 - \frac{11 \times 12}{2}}{\sqrt{\frac{11 \times 12 (11 + 12 + 1)}{12}}} = \frac{39 - 66}{\sqrt{\frac{132(24)}{12}}}
 \end{aligned}$$



2-Tail

.025

.475

.025

$$\frac{27}{\sqrt{\frac{3168}{12}}} = \frac{27}{\sqrt{264}} = \frac{27}{16.248} = -1.48$$

Table value = at 5% LOS = 1.96

Calatd value  $-1.48 <$  Table value Accept  $H_0$ .

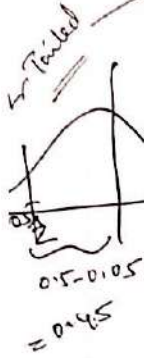
∴ There is no diff b/w 2 types.

Note

$$\left[ \begin{array}{l} \bullet \quad 1.9 \pm 0.06 \\ \text{Table value} \quad \underline{1.96} \end{array} \right]$$

When  $n_1, n_2 \geq 8$  We need to perform Z-test

$n_1, n_2 < 8$  Use Wilcoxon Table.



## Mc. Nemar Test

$$\chi^2 = \frac{(|A-D| - 1)^2}{A+D}$$

Degree of freedom =  $(r-1)(c-1)$

Terms used in Qstn  $\Rightarrow$  Before, After.


Rules

If  $Cal <$  Table (Accept  $H_0$ )  
 $Cal >$  Table (Reject  $H_0$ )

A

(\*)

In a certain before & after experiment the responses obtained from 100 respondents when classified gave the following information

		After treatment	
		Unfavourable response	Favourable response
Before treatment	Favourable response	100 (A)	200 (B)
	Unfavourable response	300 (C)	50 (D)

Test @ 5% LOS whether there has been a significant diff in ppl's attitude before & after concerning experiment.

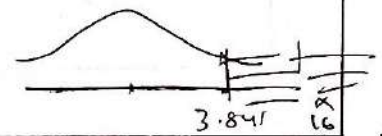
Sol :-

$H_0$  - There is no diff b/w peoples attitude  
 $H_1$  :- There is diff b/w ppl's attitude.

$$\chi^2 = \frac{(A-D-1)^2}{A+D} = \frac{(|100-50|-1)^2}{100+50} = 16$$

$$D.O.F = (r-1)(c-1) = (2-1)(2-1) = 1$$

$$\chi^2_{Table} = 3.841 \quad \text{at } 2.05 \cdot 0.5 =$$



As the Chi-square calculated value (16) is greater than Chi-square table value (3.841) at 5% LOS.  $\therefore$  Reject  $H_0$  & Accept  $H_1$ .  
 There is a significant diff in ppl's attitude b4 & after trmt.

(\*) In a certain Before & After experiment the responses obtained from 2000 respondents are classified. Test @ 5% LOS whether there has been any change in the salesmen b4 & after training.

After training.

		After training.	
		Fav <sup>r</sup> Responses	Unfav <sup>r</sup> Response
Before Training	Fav <sup>r</sup> Res	200 (A)	800 (B)
	Unfav <sup>r</sup> Res	600 (C)	900 (D)

Sol  $H_0$  - There is no diff b/w B, A Exp  
 $H_1$  - " " diff b/w " "

$$K^2_{(cal)} = \frac{(A-D-1)^2}{A+D} = \frac{(200-900-1)^2}{200+900} = 66$$



$$DOF = (r-1)(c-1) = (2-1)(2-1) = 1$$

$$\chi^2_{\text{Tabl}} = 3.841 @ 5\% \text{ LOS}$$

con - Rejected  $H_0$ . As  $\chi^2_{\text{cal}} > \chi^2_{\text{Tabl}}$ .  
 $\therefore$  There is significant diff b/w bt & after training of salesmen.

## Kruskal Wallis Test

### K-H Test (H test)

3 or more samples

$$H = \left[ \frac{12}{N(N+1)} \left[ \frac{R_1^2}{n_1} + \frac{R_2^2}{n_2} + \dots + \frac{R_n^2}{n_i} \right] - 3(N+1) \right]$$

(\*) Using H-test find whether the 3 methods are equally effctv.

Method A - 80, 83, 79, 85, 90, 68  $n_1=6$

B - 82, 84, 60, 72, 86, 67, 91  $n_2=7$

C - 93, 65, 77, 78, 88  $n_3=5$

Sol :-  $H_0$  - There is no diff b/w 3 methods  
 $H_1$  - " " diff " "

Sol :-

Step 1 -

Arrange all numbers in ascending order.

60	65	67	68	72	77	78	79	80
B	C	B	A	B	C	C	A	A
1	2	3	4	5	6	7	8	9
82	83	84	85	86	88	90	91	
B	A	B	A	B	C	A	B	
10	11	12	13	14	15	16	17	
93								
C								
18								

$$R_1 \Rightarrow \text{Ranks of A} = 4 + 8 + 9 + 11 + 13 + 16 = 61$$

$$R_2 \Rightarrow \text{Ranks of B} = 1 + 3 + 5 + 10 + 12 + 14 + 17 = 62$$

$$R_3 \Rightarrow \text{Ranks of C} = 2 + 6 + 7 + 15 + 18 = 48$$

$$n_1 = \text{No. of observations (A)} = 6$$

$$n_2 = \text{ " (B)} = 7$$

$$n_3 = \text{ " (C)} = 5$$

$$N = n_1 + n_2 + n_3 = 6 + 7 + 5 = 18$$



$$\begin{aligned}
 H &= \left[ \frac{12}{N(N+1)} \left[ \frac{R_1^2}{n_1} + \frac{R_2^2}{n_2} + \frac{R_3^2}{n_3} \right] - 3(N+1) \right] \\
 &= \frac{12}{18(18+1)} \left[ \frac{(61)^2}{6} + \frac{(62)^2}{7} + \frac{(48)^2}{5} \right] - 3(18+1) \\
 &= \left[ \frac{12}{342} (620.17 + 549.14 + 460.8) - 3(19) \right] \\
 &= \left[ 0.035 (1630.11 - 3(19)) \right] \\
 &= 57.054 - 57 \\
 &= 0.0535
 \end{aligned}$$

Degree of Freedom  $\Rightarrow k-1 =$   
 $k = \text{No. of samples}$   
 $= 3-1$   
 $= 2$

Chi-Sq Tab Val @ 5% LOS at 2 D.O.F  
 is 5.991

Cal As  $H_{cal} (0.0535) < H_{tab} (5.991)$   
 Accept  $H_0 \Rightarrow$  There is no significant Diff  
 b/w 3 methods.

⊗ A training was conducted for salesmen the method of training used is different from each group. find is there any diffc in training methods.

A	75	83	68	85	90	61	$n_1=6$
B	62	70	67	82	80	87	$n_2=7$
C	65	71	74	63	89		$n_3=5$

Sol :-  $H_0$  - There is no diff in traing methods  
 $H_1$  - " " " " diff.

Step 1 Arrange in AO.

61	62	63	64	65	67	68	70	70
A	B	C	B	C	B	A	B	C
1	2	3	4	5	6	7	8	9
74	75	80	82	83	85	87	89	
C	A	B	B	A	A	B	C	
10	10	12	13	14	15	16	17	
90								
A								
18								

Step 2: Sum of Ranks.

R<sub>1</sub> (A) = 1+7+11+14+15+18 = 66.

R<sub>2</sub> (B) = 2+4+6+8+12+13+16 = 61

R<sub>3</sub> (C) = 3+5+9+10+17 = 49

N = n<sub>1</sub> + n<sub>2</sub> + n<sub>3</sub> = 6+7+5 = 18.

H = [ 12 / (N(N+1)) \* ( R<sub>1</sub><sup>2</sup>/n<sub>1</sub> + R<sub>2</sub><sup>2</sup>/n<sub>2</sub> + R<sub>3</sub><sup>2</sup>/n<sub>3</sub> ) - 3(N+1) ]

= [ 12 / (18(18+1)) \* ( (66)<sup>2</sup>/6 + (61)<sup>2</sup>/7 + (44)<sup>2</sup>/5 ) - 3(18+1) ]

= [ 12 / 342 \* ( 726 + 531.57 + 387.2 ) - 3(19) ]

= 0.56.

χ table 5%. (k-1) = (3-1) u = 2 ⇒ 5.991 (Tab) (val)

χ<sub>calva</sub> (0.56) < χ<sub>tabv</sub> (5.991)

Accept H<sub>0</sub> ⇒ There is no diff in the training methods.



# SIGN TEST

## CASE 1

$$n < 20.$$

$$k = \frac{(n-1)}{2} - 0.98\sqrt{n}$$

$n$  = Sample size

Compare  $k$  value with  $S$

$S$  = No. of Negative signs

$S > k$  (Accept  $H_0$ ).

$S \leq k$  [Reject  $H_0$ ].

## CASE 2

$$n > 20$$

$$Z = \frac{x - np_0}{\sqrt{np_0(1-p_0)}}$$

$$P_0 = 0.5$$

$n$  = Sample size

$x$  = No. of +ve signs

Compare with  $Z$ -table.

(\*) Use the sign test to see if there is any difference b/w no. of days until the collection of an A's Rowl b4 & after a new collection policy Use s/l os

Before	30	28	34	35	40	42		
After	32	29	33	32	37	43		
	-	-	+	+	+	-		
B4	33	38	34	45	28	27	25	41
								36
After	40	41	37	44	27	33	30	38
	-	-	-	+	+	-	-	+
								0

$H_0$  - There is not any diff b/w A & B

$H_1$  - There is

$$n=12$$

$$k = \frac{(n-1)}{2} - 0.98\sqrt{n}$$

$$= \frac{12-1}{2} - 0.98\sqrt{12}$$

$$= 5.5 - 0.98(3.46)$$

$$= 5.5 - 3.3908$$

$$= 2.11$$

$\therefore$  There is diff b/w 2 brands.

$S$  = No. of -ve signs

$$= 2$$

$$K > S$$

$$(2.11) > (2)$$

Accept  $H_1$   
reject  $H_0$ .

⊗ Find if there any difference b/w 2 methods by using the sign test.

Method A	Method B	
58	32	+
60	48	+
42	50	-
62	41	+
65	45	+
59	40	+
60	43	+
52	43	+
50	70	-
75	60	+
59	80	-
52	45	+

$H_0$  - There is no significant difference between the Alcs Revbl

$H_1$  - There is difference.

$$n = 15$$

$$n = 15 - 1 = 14 \quad (\text{beoz 1 value is 0 } 36 - 36 = 0)$$

$$K = \frac{(n-1)}{2} - 0.98 \sqrt{n}$$

$$= \frac{14-1}{2} - 0.98 \sqrt{14}$$

$$= 6.5 - 3.67$$

$$= 2.83.$$

$$S = -ve \text{ sign } No. \\ = 8$$

$K < S$  So Accept  
( $2.83 < 8$ )  
 $H_0$ .

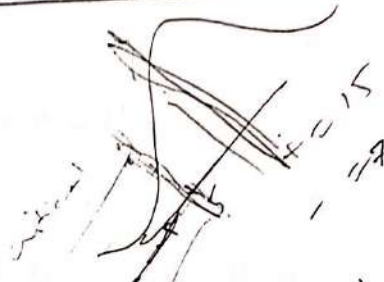
Con: There is no diff b/w the Alcs Revbl.

⊗ Find is there any difference b/w the two brands A & B by using the sign test.

BRAND A	26	30	94	23	18	50	16	25
Brand B.	22	27	39	7	11	56	19	18
	+	+	+	+	+	-	+	+
	49	37	20					
	51	33	16					
	-	+	+					



57	36	+
30	56	-
46	40	+
66	70	-
40	50	-
78	53	+
55	50	+
52	30	+
58	42	+
44	45	-



$$x_{\text{cal}} = \text{Min}(15, 7)$$

$$x_{\text{Tab}} = 5$$

$n = 22$   
 $\alpha = 0.05$   
 $x_{\text{Tab}} = 5$   
 $x_{\text{cal}} > x_{\text{Tab}} \rightarrow \text{Accept } H_0$

$H_0$  - There is no diff b/w 2 methods  
 $H_1$  - " " diff  
 $x$  = no. of + signs

Case 2 -

$$n > 20.$$

$$Z = \frac{x - np_0}{\sqrt{np_0(1-p_0)}} = \frac{15 - 22(0.5)}{\sqrt{22(0.5)(1-0.5)}}$$

$$= \frac{4}{\sqrt{5.5}} = \frac{4}{2.345} = 1.706.$$

$$Z_{\text{Tab}} @ 5\% \text{ LOS} = [-1.96 \text{ to } +1.96]$$

$\therefore Z_{\text{cal}} < Z_{\text{Tab}} \rightarrow \text{Reject } H_0.$

There is no diff b/w 2 methods.

## SIGN TEST FOR 1 SAMPLE

We are required to test the hypothesis  
 Let the mean value = 20 against alternate  
 hypothesis  $\mu \neq 20$ . 15 observations are  
 taken & the following results are obtained.  
 Use 5% LOS.

<del>(15-sample)</del> SAMPLE	(20-sample) SIGN
18	-
19	-
25	+
21	+
16	-
15	⊖ -
19	-
22	+
24	+
21	+
18	-
17	-
15	-
26	+
24	+
$n = 15$	$X = \text{no. of + signs} = 7$

$$Z = \frac{x - np_0}{\sqrt{np_0(1-p_0)}} = \frac{7 - 15(0.5)}{\sqrt{15(0.5)(1-0.5)}} = \frac{-0.5}{1.936} = -0.26$$

$$Z_{\text{Table value}} = [-1.96 \text{ to } +1.96]$$

As Cal. value is falling in the region  
So Accept  $H_0$ .

## RUN TEST

step 1 - find the runs

$$\text{step 2 - } \mu_r = \left[ \frac{2n_1n_2}{n_1+n_2} \right] + 1$$

$$\text{step 3 - } \sigma_r = \sqrt{\frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1+n_2)^2(n_1+n_2-1)}}$$

$$\text{step 4 - } Z_{\text{cal}} = \frac{U - \mu_r}{\sigma_r} \quad \left[ \begin{array}{l} \text{compare cal. value} \\ \text{with } Z \text{ value \& give} \\ \text{conclusion} \end{array} \right]$$

$$Z = \frac{x - np_0}{\sqrt{np_0(1-p_0)}}$$



⊗ Consider the following arrangements of patients male & female who have visited an OPD in an hospital during the first few hrs on a working day.  
 The order is as follows:-  $\left\{ \begin{array}{l} *MM \quad UD \quad TQ \quad \text{Run Test} \\ \downarrow \\ \text{cont. series} \end{array} \right\}$

$\frac{MMM}{1} \quad \frac{FF}{2} \quad \frac{MMMM}{3} \quad \frac{FFF}{4} \quad \frac{MMM}{5} \quad \frac{FFFFF}{6} \quad \frac{MM}{7}$

$U = \text{Runs} = 7$

$n_1 = 12 \text{ (M) - Male}$

$n_2 = 10 \text{ (F) - Female}$

$H_0$  - Male & female patients  
 $H_1$  - " " "

hv come in random  
 not  
 Run Table  
 $n_1 = 12, n_2 = 10$

$G_1 = 7, 18$   
 $G_2 =$

$$\mu_j = \left[ \frac{2n_1n_2}{n_1+n_2} \right] + 1$$

$$= \frac{2(12)(10)}{12+10} + 1 = 11.9$$

$G = 7$   
 $(G_1, G_2) = (7, 18)$

$$\sigma_s = \sqrt{\frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1+n_2)^2(n_1+n_2-1)}} = 2.27$$

$$Z = \frac{U - \mu_r}{\sigma_r} \Rightarrow \frac{7 - 11.9}{2.27} = (-2.16)$$

Conclusion: Accept  $H_0$

$G = 7$  lies in d  
 critical region  
 Reject  $H_0$



x) The foll. arrangement shows the rise (U) & fall (d) in the price of equity shares on 40 consecutive days on which its price did not remain the same.

$\frac{UU}{1}$     $\frac{DD}{2}$     $\frac{UUU}{3}$     $\frac{D}{4}$     $\frac{UUU}{5}$     $\frac{DD}{6}$     $\frac{U}{7}$     $\frac{DDD}{8}$     $\frac{U}{9}$     $\frac{DD}{10}$   
 $\frac{U}{11}$     $\frac{DD}{12}$     $\frac{UUUU}{13}$     $\frac{DDDD}{14}$     $\frac{UU}{15}$     $\frac{D}{16}$     $\frac{UU}{17}$     $\frac{DDD}{18}$     $\frac{U}{19}$

$H_0$  - Let there be no diff b/w price rise & fall (random)

$H_1$  - Let " " diff " " (2-tailed)

$U = 19, n_1 = 20 (U) \quad n_2 = 20 (D)$

$$\mu_r = \left[ \frac{2n_1n_2}{n_1+n_2} \right] + 1 = 21$$

$$\sigma_r = \sqrt{\frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1+n_2)^2 (n_1+n_2 - 1)}} = 3.12$$

$$Z = \frac{\mu - \mu_r}{\sigma_r} = -0.64$$

$Z_{table}$  at 0.05 LOS =  $\pm 1.96$

$$Z_{cal} = -0.64$$

$|Z_{cal}| < Z_{Table}$   
 $0.64 < 1.96$  - Accept  $H_0$

# Wilcoxon Matched Pair Test.

$n < 25$  (Wilcoxon table)

\* 2 models of machines are under consideration for purchase & the org. has 10 of each for a trial period & the team of 19 operators for each machine for a fix length of time. find using WMP T is there any diff b/w 2 m/c's.

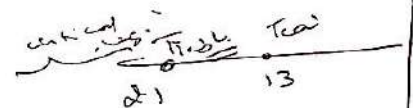
operations	M/c I	M/c II	di Diff	diff Ranks	Ranks with +	Ranks with -
			18	11	11	
A	78	60	17	10	10	
B	75	58	17	7	7	-3
C	53	46	7	-3	-	
D	68	71	-3	2	2	
E	82	80	2	5	5	
F	64	59	5	13	13	
G	95	73	22	8	8	
H	86	78	8	14	14	
I	64	37	27	-4	-	-4
J	71	75	-4	-4	-	-6
K	54	60	-6	-6	-	
L	80	79	1	1	1	
M	51	38	13	9	9	
N	70	51	19	12	12	
				92	92	13

$N = 14$

Minimum Value (absolute) (13)  $T_{cal} = 13$

$T_{tab} = n = 14 =$  Table value = 21

Calc Table Accept  $H_0$ .





For wilcoxon test if  $T_{cal}$  value is less than or equal to Table value (~~accept  $H_0$~~ ) reject  $H_0$ .

If  $T_{cal} \leq T_{tab}$  (Reject  $H_0$ ) ✓

$T_{cal} > T_{tab}$  Accept  $H_0$

$T_{cal} < T_{tab}$  Reject  $H_0$

concl: As  $T_{cal} < T_{tab}$  reject null hyp.

∴ Test statistic  $T$  is smaller of  $T^+$  &  $T^-$  critical region is in left hand tail

⊗ A manufg. electric toys has been taken over by another co. workers were appld to ascertain their satisfctn level. The same wkrs wr again approach to know their satisfctn after d takeover of d co. find usg wilcoxon matched pair test whether there is an impmnt in d satisfctn of wkrs after d takeover of d co.

$H_0$ : There is no signifc diff in d satisfctn of wkrs after d takeover of d co.

$H_1$ : There is diffc.

B4	After	Diff	Ranks	Ranks $v_{th}^+$	Ranks $v_{th}^-$
		4	5	5	-
69	65	-2	4	-	-4
73	75	-5	9	-	-9
58	63	1	1.5	1.5	-
76	78	0	-	-	-
82	82	0	-	-	-
65	68	-3	5	-	-5
75	71	4	5	5	-
64	65	-1	1.5	-	-1.5
87	85	2	4	4	-
70	68	2	4	4	-
				29.5	-19.5

Min value  $T_{cal} = 19.5$

$n = 10 - 1 = 9$

$T_{tab} = 6$

$T_{cal} > T_{tab}$  val



$$20.5 > 6$$

Accept  $H_0$

⊗ Find is there any significant diff b/w 2 brands  
by using WMPT

Brand A	Brand B	Diff	Ranks	Ranks $v_{th} +$	Ranks $v_{th} -$
		4	5.5	5.5	
26	22	4	3	3	
30	27	3	8	8	
44	39	5		11	
23	7	16	11		
18	11	7	9.5	9.5	-12
50	56	-41	-12	-	
34	30	4	5.5	5.5	
16	14	2	1.5	1.5	
25	18	-1	9.5	9.5	
49	51	-2	-1.5	-	-1.5
37	33	4	5.5	5.5	
20	16	4	5.5	5.5	
				64.5	-13.5

$$\text{Min Value}(T_{cal}) = | -13.5 | = 13.5$$

$$T_{tab} \quad n = 12$$

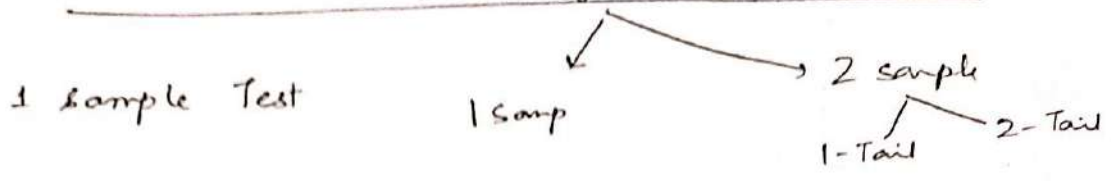
$$\text{Value} = 14$$

$$T_{cal} < T_{tab}$$

$$13.5 < 14$$

∴ Reject  $H_0$ .

K-S Test Kolmogorov Smirnov Test



The table below provide info pertaining to observers freq list of daily visits of customers to the showroom list with this freq distr follows poisson disbtr or not LOS = 5%.

No. of visits	No. of Days	Com. freq	Relativ com freq	Expected freq	com Expected freq	Rfo - Rfe
0	5	5	$\frac{5}{100} = 0.05$	0.018	0.018	0.03
1	25	30	$\frac{30}{100} = 0.30$	0.072	0.09	0.21
2	19	49	$\frac{49}{100} = 0.49$	0.144	0.234	0.251
3	29	78	$\frac{78}{100} = 0.78$	0.192	0.426	<b>0.354</b> →
4	3	81	$\frac{81}{100} = 0.81$	0.192	0.618	0.192
5	10	91	$\frac{91}{100} = 0.91$	0.154	0.772	0.138
6	9	100	$\frac{100}{100} = 1$	0.102	0.874	0.128

7 100  
 Highest value of D is  
 D value = 0.354

$D_{calcd} = 0.354$

~~$H_0$ : does not follow P.D.~~  
 ~~$H_1$ : follows P.D.~~

$H_0$ : → Given frequency follows P.D.  
 $H_1$ : → does not follow P.D.

Poisson Distribution

$$\frac{e^{-\lambda} \lambda^x}{x!} \quad \lambda = 4$$

Expected freq. =

$$P(x=0) = \frac{e^{-4} \cdot 4^0}{0!} = 0.018$$

$$P(x=1) = \frac{e^{-4} \cdot 4^1}{1!} = 0.018 \times 4 = 0.072$$

$$P(x=2) = \frac{e^{-4} \cdot 4^2}{2!} = \frac{0.018 \times 16}{2} = 0.144$$

$$P(x=3) = \frac{e^{-4} \cdot 4^3}{3!} = \frac{0.018 \times 4^3}{3 \times 2 \times 1} = 0.192$$

$$P(x=4) = \frac{e^{-4} \cdot 4^4}{4!} = \frac{4.608}{24} = 0.192 \quad \rightarrow \frac{0.018 \times 4^4}{4 \times 3 \times 2 \times 1}$$

$$P(x=5) = \frac{18.432}{120} = 0.154$$

$$P(x=6) = \frac{73.728}{720} = 0.102$$

$$D_{cal} = 0.354$$

$$D_{tab} = 0.136$$

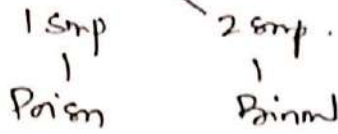
NC 35 <sup>use</sup> (Z-table)

N > 100	
5%	1%
1.36 $\frac{1.36}{\sqrt{N}}$	1.63 $\frac{1.63}{\sqrt{N}}$

- In d word binomial & poisson is not mentioned then use rule of homogeneity to calculate expd freqy  
 $\therefore D_{cal} > D_{tab}$  Reject  $H_0$  & Accept  $H_1$   
 Given frequency distribtn does not follow a Poisson distribution



# K-S Test



→ Rule of Homogeneity.

x) A research is conducted by taking sample of 250 respondents to find the pref of customers towards its task.

$H_0$ : let there be no right, diff in d customers pref towards taste

$H_1$ : let there be

	freq	① Cum freq	② $R_{fo}$ $\frac{R_{fo}}{\text{Cum freq}}$ $60 \div 250$	③ $\frac{250}{5} = 50$ Exptd freq.	④ Cum Exp freq.
1	60	60	0.24	50	50
2	70	130	0.52	50	100
3	30	160	0.64	50	150
4	50	210	0.84	50	200
5	40	250	1.0	50	250
	<u>250</u>				

⑤  $R_{fe}$

$R_{fo}$	Exp Com freq
0.2	$50 \div 250$
0.4	$(100/250)$
0.6	$(150/250)$
0.8	$(200/250)$
1.0	$(250/250)$

⑥ = ② - ⑤

$R_{fo} - R_{fe}$

0.04
0.12
0.04
0.04
0

Dcal value is the highest table value  
 i.e 0.12  
 $N > 35$  ? D-table  
 $\frac{1.36}{\sqrt{N}}$  Los 5%  
 $= \frac{1.36}{\sqrt{250}} = 0.086$   
 $D_{vc} = 0.12$   
 $D_t = 0.086$



conclusion:

Deal val (0.12) is more than D table value 0.086.  
 So Reject  $H_0$  i.e. there is a diff in d cust.  
 pref towards tastes.

Because 1, 2, 3 is not given directly scores - given so do  
 in form  $\downarrow$

Use K-S test @ 5% LOS to test whether the  
 distribtn is uniform. don't consider  
-ve sign.

SCORES	$O_i$ Freq	Cum Freq	$A_i$ Relative freq	$ A_i - Q $
41	2	2	$2 \div 25 = 0.08$	$1.92 - 0.08 = 2$
42	3	5	0.2	2.8
43	1	6	0.24	0.76
44	4	10	0.4	<b>3.6</b>
45	2	12	0.48	1.52
46	2	14	0.56	1.44
47	4	18	0.72	3.28
48	2	20	0.8	1.2
49	4	24	0.96	3.04
50	1	25	1	0
	25			

see highest  
 value that  
 will be  
 deal val = 3.6

$F_{0.05}$   
 2.5  
 2.5

2.5  
 5  
 7.5  
 10  
 12.5  
 15

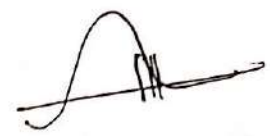
$H_0$ : Is uniform  
 $H_1$ : Is not uniform

$$D_{table} \ 5\% = \frac{1.36}{\sqrt{n}} = \frac{1.36}{\sqrt{10}} = 0.43$$

Cal val <sup>3.6</sup> > Tab <sup>0.43</sup> Rejected H<sub>0</sub>.

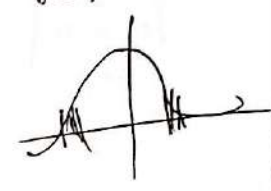
Q) K.S 2 Sample Test - one Tailed

$$\chi^2_{cal} \Rightarrow 4D^2 \left| \frac{n_1 n_2}{n_1 + n_2} \right|$$



K.S Two Sample Test - Two Tailed Test

$$\chi^2_{cal} = \frac{1.36 \sqrt{n_1 + n_2}}{n_1 n_2}$$



⇒ 2-Tail test

Use K-S test @ 5% LOS to test whether there is diff in scores of two departments 2 sample

Scores	dep A	dep B
30-35	5	6
35-40	4	16
40-45	6	2
45-50	7	8
50-55	2	10
55-60	2	15
60-65	4	13

$H_0$  - Let there be no sig. diff b/w the scores of 2 deptchs.  
 $H_1$  - be a

Scores	Dep A	Cum freq	$R_{fo}$ Rel Cf	Dep B	Cum freq	$R_{fc}$ Rel Cf	$R_{fo} - R_{fc}$
30-35	5	5	$\frac{5}{30} = 0.167$	6	6	$\frac{6}{70} = 0.086$	0.081
35-40	4	9	0.3	16	22	0.31	- 0.01
40-45	6	15	0.5	2	24	0.34	0.16
45-50	7	22	0.73	8	32	0.46	0.27 - D
50-55	2	24	0.8	10	42	0.6	0.2
55-60	2	26	0.87	15	57	0.8	0.07
60-65	4	30	1.0	13	70	1.0	0
	$n_1 = 30$			$n_2 = 70$			

One tail test

$\mu_A - \mu_B > \mu_B$

$\mu_A - \mu_B = \mu_B$

$H_1 - \mu_A \neq \mu_B$

$\mu_1 -$

KS Two sample test - Two Tailed test

$$\chi^2_{\text{cal}} = \frac{1.36 \sqrt{n_1 + n_2}}{n_1 n_2} = \frac{1.36 \sqrt{30 + 70}}{30 \times 70} = 0.07$$

$D_{\text{cal}} = 0.27 > D_{\text{tab}} = 0.07$  Accept  $H_1$

Q. Test @ 5% LOS whether the scores of dep A is higher than the scores of dep B case - k-s one-tail (15)

Marks	Sec A	Sec B
30-40	3	4
40-50	12	13
50-60	12	13
60-70	4	3
70-80	2	1
80-90	5	5
90-100	2	1

H<sub>0</sub> - Let there be no significant diff b/w the scores obtained by 2 Dep.

H<sub>1</sub> ⇒ Let scores of Dep A > Dep B



Test whether the 2 samples have come from the same population or not by applying Mann whit

SAMPLE 1	SAMPLE 2	S <sub>1</sub>	S <sub>2</sub>	RANK	RANK	R	S <sub>1</sub> CR X DIGIT	S <sub>2</sub> CR X DIGIT
57	61	-	32	1	1	-	-	1x1=1
39	52	38	-	2	2	2x1=2	-	-
60	41	39, 39	-	3, 4	3, 5	3.5x2=7	-	-
78	40	-	40	5	5	-	-	5x1=5
74	32	-	41	6	6	-	-	6x1=6
53	72	-	44, 44	7, 8	7.5	-	-	7.5x2=15
73	53	46	-	9	9	9x1=9	-	-
38	44	48	-	10	10	10x1=10	-	-
69	72	-	52	11	11	-	-	11x1=11
46	67	53	53	12, 13	12.5	12.5x1=12.5	12.5x1=12.5	12.5x1=12.5
39	44	57	-	14	14	14x1=14	-	-
48	70	60	-	15	15	15x1=15	-	-
12	12	-	61	16	16	-	-	16x1=16
-	-	-	67	17	17	-	-	-
-	-	-	70	18	18	18x1=18	-	-
69	70	-	70	19	19	-	-	19x1=19
-	72, 72	-	72, 72	20, 21	20.5	-	-	20.5x2=41
-	-	-	-	22	22	22x1=22	-	-
73	-	-	-	23	23	23x1=23	-	-
74	-	-	-	24	24	24x1=24	-	-
78	-	-	-	-	-	R <sub>1</sub> =156.5	-	R <sub>2</sub> =143.5

$$U_1 = n_1 n_2 + \frac{n_1(n_1+1)}{2} - R_1$$

$$= 12 \times 12 + \frac{12(12+1)}{2} - 156.5$$

$$= 222 - 156.5 = 65.5$$

$$U_2 = n_1 n_2 + \frac{n_2(n_2+1)}{2} - R_2$$

$$= 12 \times 12 + \frac{12(12+1)}{2} - 143.5 = 222 - 143.5 = 78.5$$

$$U = \min(U_1, U_2) = \frac{65.5}{(65.5, 78.5)}$$

$$Z = \frac{U - n_1 n_2 / 2}{\sqrt{n_1 n_2 (n_1 + n_2 + 1) / 12}}$$

$$= \frac{65.5 - 12 \times 12 / 2}{\sqrt{12 \times 12 (12 + 12 + 1) / 12}} = \frac{6.5}{300} = -0.02$$

Condn Acpt  $H_0$  i.e.  $(-0.02) < 1.96$  (5% LOS)

~~$H_0$ : There is no significant diff b/w the AT's~~

~~$H_1$ : There is significant diff~~

$$n = 15$$

~~$n = 15 - 1$  because value is 0 i.e.  $36 - 36 = 0$~~

$$n = 14$$

$$K = \frac{n-1}{2} - 0.98 \sqrt{n}$$

$$= \frac{14-1}{2} - 0.98 \sqrt{14}$$

$$= 6.5 - 3.67$$

$$= 2.83$$

$\therefore H_0 = \text{Acpt}$   
i.e.  $K < 8(s)$

~~Condn: There is a diff b/w the AT's~~  
~~Revol~~

Klausur

Mathematik

M → 72, 80, 83, 75

S → 81, 74, 77

Eng → 88, 82, 90, 87, 80

Econ → 90, 71, 77, 76

ag.

	1	2	3	4	5	6.5	6.5
	70	71	72	74	75	77	77
	Ec	Ec	M	S	M	S	Eco
	8.5	8.5	10	11	12	13	14
	80	80	81	82	83	87	88
	M	Eng	S	Eng	M	Eng	
		15.5	15.5				
		90	90				
		Eng	Econ				

$$R_1 \rightarrow 3 + 8.5 + 12 + 5 = 28.5$$

$$R_2 \rightarrow 10 + 4 + 6.5 = 20.5$$

$$R_3 \rightarrow 14 + 11 + 15.5 + 13 + 8.5 = 61$$

$$R_4 \rightarrow 15.5 + 2 + 6.5 + 1 = 25$$

$$n_1 = 4$$

$$n_2 = 3$$

$$n_3 = 5$$

$$n_4 = 4$$

$$N = 16$$

$$H = \left[ \frac{12}{16 \times 17} \left[ \frac{(28.5)^2}{4} + \frac{(20.5)^2}{3} + \frac{(61)^2}{5} + \frac{(25)^2}{4} - 3(17) \right] \right]$$

$$= \frac{12}{16 \times 17} \left[ \frac{812.25}{4} + \frac{420.25}{3} + \frac{3721}{5} + \frac{625}{4} - 51 \right]$$

$$= 27.15 \left[ 203.0625 + 140.083 + 744.2 + 156.25 - 51 \right]$$

$$= 27.15 \left[ 1243.5975 - 51 \right]$$

$$= 32379$$

$$D.O.F = 4 - 1 = 3$$

25/10 (100)